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# **Application of Sluice Gate in Different Positions and Its Effect on Hydraulic Parameters in Free-Flow Conditions**

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### Abstract

Underpass gates are hydraulic structures in which water moves under the gate. Here, different models of gate position including vertical, deflection to upstream and downstream of the channel with respect to the vertical axis and also oblique position concerning the transverse axis at angles of 10°, 20° and 30° was investigated numerically with FLOW-3D software. Also its effect on discharge coefficient ( $C_d$ ) and hydrodynamic force applied to the gate was checked. The nested mesh was used for modeling. The results indicated that the statistical indices such as Absolute Error (AE), percentage Relative Error (RE%) and Root Mean Square Error (RMSE) in the RNG turbulence model were less than those of the k- $\varepsilon$ , k- $\omega$  and Large Eddy Simulation (LES) and were more accurate compared to the experimental results.  $C_d$  in the same discharges increases with the increasing angle to the upstream of the channel compared to the vertical position.  $C_d$  is inversely related to increasing the angle of the gate relative to the vertical axis in the downward position. In the oblique position,  $C_d$  decreases with increasing angle to the transverse axis of the channel due to the increase in the area of flow through the gate. This increase in angle and area of the flow passing through the gate leads to a decrease in the upstream fluid depth, therefore, less hydrodynamic force is applied to the gate. The upward inclined gate tolerates less hydrodynamic force than the downward and oblique positions. The maximum value is related to the downward position.

Keywords: Sluice Gate, Stage-Discharge, Discharge Coefficient, Hydrodynamic Force, VOF

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# **1. Introduction**

Typically, the structure that determines the relationship between discharge and depth of flow in its vicinity is called the control structure. Among the flow control structures are sluice gates that have different shapes and functions hence they are used in different situations. To prevent

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water wastage, extreme care should be taken in controlling and distributing water in irrigation networks, and flow control structures such as gates should be selected correctly and following the conditions of each region. Principled design of such structures requires knowledge of hydraulic relationships and their calculation. Various researches have been done in the field of sluice gates to determine the discharge coefficient. Henry [1] deduced a diagram in which he expressed the changes in the discharge coefficient with the ratio of the upstream fluid depth to the gate opening for free-flow conditions. Rajaratnam and Subramanya [2] investigated the sluice gate discharge coefficient and confirmed (Henry [1]) results. Swamee [3] obtained the discharge coefficient of sluice gates as a function of upstream water depth and gate opening under free-flow conditions. Shivapur and Prakash [4] examined the placement of the sluice gates at different angles and provided a relationship to determine the amount of  $C_d$ . Nasehi Oskuyi and Salmasi [5] obtained the discharge coefficient of vertical sluice gates using Mathematica software. The results of their study were in good agreement with the diagram of Henry [1]. Mohammed and Moayed [6] investigated the effect of the gate edge shape and its deviation in the direction and opposite direction of flow. The results showed that  $C_d$  in the gate with an angle of 45 degrees in the flow direction and with a horizontal and sharp edge is 17.8% and 17% higher than the vertical gate, respectively. Daneshfaraz et al. [7] numerically investigated the effect of sluice gate edge shapes on flow characteristics. Their results indicated that the flow contraction coefficient for sharp edges and round-edge gates decreases when the ratio of gate opening to upstream specific energy is less than 0.4 and increases for the ratios greater than 0.4. Ashkan et al. [8] investigated the performance of consecutive sluice gates in regulating the discharge in channels using FLOW-3D software. Their results indicated that consecutive gates act with acceptable accuracy in the delivery of constant discharge in exchange for changes at upstream flow depth. Salmasi et al. [9] used experimental data and intelligence models to investigate  $C_d$  of inclined sluice gates. They concluded that the discharge coefficient increases with increasing gate placement angle.

In the case of vertical sluice gates, various numerical studies have been done including Ma et al. [10] which investigated the turbulence properties of hydraulic jumps using the standard k-ε turbulence model. Akoz et al. [11] performed experimental and numerical analysis of flow in sluice gates. Cassan and Belaud [12] examined the flow structure under sluice gates to confirm common assumptions about contraction coefficient and energy losses. Ghaderi et al. [13] numerically simulated free and submerged hydraulic jumps on different shapes of roughness in different roughness arrangements and different Froude number conditions in vertical sluice gate. Their results showed that the numerical model is well able to simulate the characteristics of the free and submerged jump. Ghaderi et al. [14] using FLOW-3D software investigated the effect of triangular roughness on jump characteristics, including longitudinal characteristics of streamlines, flow patterns in the cavity area, horizontal velocity profiles and velocity distribution in the direction of flow. Daneshfaraz et al. [15] examined the vertical gate flow in crescentshaped contractions. The results showed that the effect of crescent-shaped contraction is greater than the sudden contraction of previous studies. A review of previous studies showed that so far, no study has been done on inclined and oblique gates using VOF method, and the report of the results of this type of gate is empty among scientific sources Also, carefully in the background of the research, there is a need to study the position of the gate and its effect on hydraulic capacity, corresponding discharge coefficients and hydrodynamic force on the gate at angles and type of gate placement. Therefore, considering the importance of the problem and how to respond FLOW-3D software in simulating the flow through the sluice gate, the necessity of sluice gate geometry, including an inclination to the upstream and downstream of the channel

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and the oblique gates with different angles with respect to the vertical and transverse axis were investigated and compared with other researchers work.

# 2. Materials and methods

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## 2.1. Flow governing equations

FLOW-3D software is a good alternative to physical models in solving fluid mechanics and hydrodynamics problems. This 3D software simplifies modeling and analysis of fluid behavior by using numerical methods. FLOW-3D software is an accurate and fast software that solves the difficult free-surface flow problems. The continuity and Navier-Stokes equations are discretized by FLOW-3D software to perform three-dimensional simulation of fluid motion. The continuity equation in a fluid stream is as follows (Flow Science Inc, [16]).

$$\frac{\partial \rho}{\partial t} + \frac{\partial}{\partial x_i} (\rho u_i) = 0 \tag{1}$$

where  $u_i$  is the velocity component of the direction *i*. FLOW-3D software solves the Navier-Stokes equations for three-dimensional flow analysis using the VOF on a networked field. The equations in the Cartesian coordinate system are obtained by the following equations (Flow Science Inc, [16]).

$$V_F \frac{\partial \rho}{\partial t} + \frac{\partial}{\partial x} (\rho u A_x) + R \frac{\partial}{\partial y} (\rho v A_y) + \frac{\partial}{\partial z} (\rho w A_z) = R_{SOR} + R_{DIF}$$
(2)

$$\frac{\partial u}{\partial t} + \frac{1}{V_F} \left( uA_x \frac{\partial u}{\partial x} + vA_y \frac{\partial u}{\partial y} + wA_z \frac{\partial u}{\partial z} \right) = -\frac{1}{\rho} \frac{\partial P}{\partial x} + G_x + f_x$$
(3)

$$\frac{\partial v}{\partial t} + \frac{1}{V_F} \left( uA_x \frac{\partial v}{\partial x} + vA_y \frac{\partial v}{\partial y} + wA_z \frac{\partial v}{\partial z} \right) = -\frac{1}{\rho} \frac{\partial P}{\partial y} + G_y + f_y \tag{4}$$

$$\frac{\partial w}{\partial t} + \frac{1}{V_F} \left( uA_x \frac{\partial w}{\partial x} + vA_y \frac{\partial w}{\partial y} + wA_z \frac{\partial w}{\partial z} \right) = -\frac{1}{\rho} \frac{\partial P}{\partial z} + G_z + f_z$$
(5)

In the above relations, u, v and w are velocity components,  $A_x$ ,  $A_y$  and  $A_z$  are a fraction of the area associated with the flow,  $G_x$ ,  $G_y$  and  $G_z$  are the body acceleration,  $f_x$ ,  $f_y$ , and  $f_z$  are the viscosity acceleration in the directions of x, y and z,  $R_{SOR}$  is the mass source,  $R_{DIF}$  is the expression of turbulence,  $V_F$  is the fluid volume fraction, and P is the pressure. This equation is generally expressed as equation (6).

$$\rho\left(\frac{\partial u_i}{\partial t} + u_j\frac{\partial u_i}{\partial x_i}\right) = -\frac{\partial P}{\partial x_i} + B_i + \frac{\partial}{\partial x_j}\left[\mu\left(\frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} - \frac{2}{3}\delta_{ij}\frac{\partial u_k}{\partial x_k}\right)\right]$$
(6)

where  $B_i$  is the volumetric force in direction *i* and  $\mu$  is the dynamic viscosity of the fluid,  $\rho$  is the water density,  $x_i$ ,  $x_j$  and  $x_k$  are the flow coordinates in the spatial direction *i*, *j* and *k*, respectively.  $\delta_{ij}$  is Kronecker delta, where, if i = j its value is equal to 1 otherwise, it has a zero value (Daneshfaraz et al. [17]).

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## 2.2. Dimensional analysis

In Figure 1, the studied models are shown in different positions of the gates, including vertical, inclined to the upstream and downstream of the channel and oblique. Figure 1 shows the most significant parameters affecting the  $C_d$  and hydrodynamic force on the gate.



Figure 1. Schematic view of the gate a) Vertical position b) Downward inclined position c) Upward inclined position d) Oblique position.

The parameters affecting the flow rate through the inclined and oblique sluice gates can be shown as equation (7):

$$f_1(C_d, y_0, G, L, \rho, \mu, g, \theta) = 0$$
<sup>(7)</sup>

In equation (7),  $C_d$  is the discharge coefficient (-),  $y_0$  is the water depth upstream of the gate (L), *G* is the gate opening (L), *L* is the gate length (L),  $\rho$  is the water density (ML<sup>-3</sup>),  $\mu$  is the dynamic viscosity (ML<sup>-1</sup>T<sup>-1</sup>), *g* is the gravitational acceleration (LT<sup>-2</sup>) and  $\theta$  is the gate angle (-). Considering  $\rho$ , *g* and  $y_0$  as iterative variables and using the  $\pi$ -Buckingham method, the dimensionless equation can be presented for the sluice gate discharge coefficient:

$$C_d = \frac{Q}{A\sqrt{2gy_0}} = f_2\left(\frac{y_0}{G} \cdot \frac{y_0}{L} \cdot Re \cdot \theta\right)$$
(8)



In equation (8),  $R_e$  represents the dimensionless Reynolds number. In the present study, the flow is turbulent and  $26361 \le R_e \le 60172$ , so the effect of Reynolds number can be ignored (Daneshfaraz et al. [18]).

In equation (8), the area of the flow (A) through the oblique gate is calculated from equation (9):

$$A = LG \tag{9}$$

To calculate the subsurface level for the non-oblique gate state, in equation (9), instead of the L parameter, the channel width parameter, ie. W(L) is used.

The value of  $C_d$  in the vertical gate position is a function of the upstream water depth and gate opening, so the most significant parameter affecting it can be expressed as equation (10) (Swamee [3]):

$$C_d = f_1(y_0, G) \tag{10}$$

According to equation (11), the hydrodynamic force applied to the sluice gate can be calculated by writing the moment equation between sections 0 and A.

$$\frac{1}{2}\gamma y_0^2 - \frac{1}{2}\gamma y_A^2 - R = \rho q (V_A - V_0)$$
(11)

where q is the discharge per unit in width of the channel ( $L^2T^{-1}$ ),  $\gamma$  is the specific weight (ML<sup>-</sup> <sup>2</sup>T<sup>-2</sup>), and R is the reaction force which is equal to the hydrodynamic force.

## 2.3. Definition of the solution network and boundary conditions

In this study, validation was performed using the experimental data of Shivapur and Prakash [4] for vertical gate, and then the simulations were continued for the studied models.

Table 1 presents the hydraulic and geometric characteristics of the studied models. Also, the three-dimensional geometry of the model and the mesh networks are shown in Figure 2.

-	Hydraulic characteristic	cs			
Upstream depth of the gate (m)	Discharge (m <sup>3</sup> /s)	Reynolds number (-)			
0.06 - 0.3	0.0053 - 0.012	26361 - 60172			
	Geometric characteristic	cs			
Channel dimensions (m)	θ (degree)	NO. Run			
		Gate placement mode	NO.		
		Vertical	33		
2×0.5×0.2	Vertical – 10 – 20 – 30	Upward inclined position	33		
		Downward inclined position	33		
		Oblique position	33		

Table 1. Hydraulic and geometric characteristics of the studied models

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Figure 2- a) Three-dimensional geometry and boundary conditions b) Mesh networks

In this research, simulations have been performed using 2 nested mesh blocks with different dimensions. To achieve the optimal mesh, simulations were performed in 4 cases with different mesh dimensions and comparing results of numerical solution with experimental results, including upstream flow depth and  $C_d$  of the sluice gate. In the present study, the statistical indices of Absolute Error (AE), percentage Relative Error (RE%), Root Mean Square Error (RMSE) and the determination coefficient (R<sup>2</sup>) were used to evaluate the model performance in simulation and compare its results with experimental results:

$$AE = |x_{exp} - x_{num}| \tag{12}$$

$$RE\% = \frac{AE}{x_{exp}} \times 100 \tag{13}$$

$$RMSE = \sqrt{\frac{\sum_{i=1}^{n} \left(x_{exp} - x_{num}\right)_{i}^{2}}{n}}$$
(14)

$$R^{2} = \left(\frac{\sum_{l=1}^{n} (X_{exp} - \overline{X_{exp}}) \times (X_{num} - \overline{X_{num}})^{2}}{\sqrt{\sum_{i=1}^{n} (X_{exp} - \overline{X_{exp}})^{2} \times \sqrt{\sum_{i=1}^{n} (X_{num} - \overline{X_{num}})^{2}}}\right)$$
(15)

In the above equations, *exp* and *num* represent the experimental and numerical results, n is the total number of data. The values of the equations (12, 13 and 14) when close to the number zero and the value of the equation (15) when closes to the number one indicates the high accuracy of the presented equations (Daneshfaraz et al. [15]).

			Table	2. Optin	nal mesh	selection	n			
Test	Size of cells(m)	Total Mesh	Max R Erro	Max Relative Error (%)		ean ative r (%)	RM	ISE	R <sup>2</sup>	
			y0	$C_d$	y0	Cd	<i>y</i> <sub>ℓ</sub> (m)	<i>C</i> <sub>d</sub> (-)	yo	Cd
1	0.005,0.01	640000	26.72	16.82	21.04	12.64	0.0436	0.0776	0.966	0.652
2	0.0045,0.009	869352	9.89	5.35	5.24	2.76	0.0104	0.0184	0.993	0.904
3	0.004,0.008	1250000	6.26	3.29	2.59	1.32	0.0054	0.0099	0.993	0.910
4	0.0035,0.007	1868581	4.93	2.56	1.88	0.95	0.0038	0.0074	0.997	0.912

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The results of the percentage Relative Error for the optimal mesh of 0.008 and 0.004 m are shown in Table 4 between the experimental and numerical data. According to Table 2 and investigating the statistical indicators, it was observed that test No.4 has desirable conditions in comparison with other test cases. The statistical indicators obtained from tests No.3 and 4 are very close to each other, therefore test No.3 is considered as the optimal mesh with mesh dimensions of 0.008 and 0.004 m to continue the simulation process of the studied models. While the difference between the total numbers of meshes between tests No.3 and 4 is 618581 meshes. The fluid range behind the gate and the hydrostatic pressure distribution was defined as the initial conditions. In selecting the boundary conditions, in the first mesh block, the volume flow rate and output boundary conditions are used for the input and end of the channel, respectively. Also, for the walls and floor, the boundary condition of the wall has been selected. For the upper, the symmetric boundary condition has been used. In addition, in the second mesh block, in order to be affected by the boundary conditions defined in the first mesh block, the symmetry boundary condition is defined for the input, output and upper boundary, and the wall condition is defined for the walls and the floor. Symmetry boundary condition considers the conditions outside the solution network similar to the conditions on the internal boundary of the network. Symmetry boundary condition acts as a mirror that reflects all the flow distribution to the other side. Another application of this type of boundary condition is at the free surface of the fluid. When the boundary condition on the boundary  $Z_{max}$  is considered symmetry (Ghaderi et al. [19]), the conditions above the fluid surface are considered to be infinitely similar to the atmospheric conditions until the flow doesn't reach this boundary. Another application of this boundary condition, which is used as a solution field in problems of more than one cube network, is to use it on the interlocking faces of two separate solution networks (mesh blocks). In this way, the flow characteristics at the boundary of the first network are assigned to the second network without change. In the present study, two nested block meshes have been used. In order to affect the second mesh block from the boundary conditions defined in the first mesh block, the symmetry boundary condition has been used.

## 2.4. Turbulence models

To select the turbulence model simulations were performed with four RNG, k- $\varepsilon$ , k- $\omega$  and LES models. Finally, the RNG turbulence model was selected to continue the simulations. There are numerous reasons for choosing this model such as reliability in answering various problems, accurate solution of equations, high accuracy in showing the details of the flow and review of previous studies (Ghaderi et al. [13], Ghaderi et al. [19]). Also, the comparison of the simulation results of the turbulence models mentioned in Table 3 shows that the RNG turbulence model has less error than other turbulence models and its results are closer to the experimental data. While other models have results close to the experimental results.

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Turbulence Model	Max Relativ (%)	ve Error	M	RE	RM	ISE	$\mathbb{R}^2$		
	y0	$C_d$	yo	Cd	<i>y</i> <sub>ℓ</sub> (m)	<i>C</i> <sub>d</sub> (-)	y0	Cd	
RNG	6.26	3.29	2.59	1.32	0.0054	0.0099	0.993	0.910	
k-ε	6.65	3.50	3.10	1.58	0.0060	0.011	0.990	0.864	
k-ω	6.89	3.63	3.40	1.74	0.0067	0.012	0.988	0.828	
LES	6.45	3.39	2.82	1.44	0.0055	0.0103	0.992	0.891	

 Table 3. Numerical solution results for different turbulence models

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#### 3. Results and Discussion

In this study, the experimental results of Shivapur and Prakash [4] were used for validation. According to Figure 3, it can be seen that there is a good agreement between the results of the experimental and numerical solution. So that the Mean Relative Error percentages, Mean Absolute Error, Root Mean Square Error between experimental and numerical solution results for the upstream depth of the gate are 2.59%, 0.0045 m and 0.0054 m, respectively, and these values are 1.32%, 0.0078 and 0.0099 for  $C_d$ , respectively. Table 4 shows the calculation of the percentage Relative Error between each experimental and numerical data for the discharge coefficient and water depth upstream of the gate in different discharges for nested mesh with sizes of 0.008 and 0.004 meters.

a)

b)



Figure 3. Comparison of a) Upstream water depth b)  $C_d$  obtained from the results of experimental and numerical solution

Table 4. Percentage relative error between experimental and numerical results for $C_d$ and $y_0$ at
different discharges

 Q (m <sup>3</sup> /s)	Cd (-) Experimen tal	C <sub>d</sub> (-) Numerical	RE (%)	yo (-) Experimen tal	y <sub>0</sub> (-) Numerica l	RE (%)
 0.00648	0.5726	0.5768	0.74	0.102	0.100	1.46
0.00751	0.5667	0.5853	3.29	0.140	0.131	6.26
0.00808	0.5811	0.5941	2.23	0.154	0.147	4.31
0.00963	0.6261	0.6155	1.68	0.188	0.195	3.46
0.00997	0.6181	0.6179	0.03	0.207	0.207	0.06
0.01060	0.6178	0.6194	0.25	0.235	0.233	0.50
0.01163	0.6196	0.6261	1.05	0.281	0.275	2.07

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According to the initial and boundary conditions, the numerical solution starts nonpermanently and continues until the flow reaches a steady state until the solution becomes stable (Figure 4-a). According to Figure 4-b, the changes in the upstream water level are shown for the discharge of 0.0075 m<sup>3</sup>/s. It is observed that over time, these changes have diminished and the water level has stabilized at a certain depth.





Figure 4. a) Discharge-time hydrograph diagram b) Three-dimensional figure of flow at different times

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#### 3.1. Upward inclined gate discharge coefficient

Figure 5-a shows the stage-discharge diagram for the vertical and inclined sluice gates with angles of 10°, 20° and 30°. At the same discharge, when the sluice gate is at an angle of 30°, the upstream water depth has the lowest value, and the highest value is related to the vertical position. In other words, by increasing the angle, the depth upstream of the gate decreases. The reason for this can be pointed to the position of the gate so that as the angle increases, the flow through the gate converges and the flow lines tend more to the outlet of the gate. It also reduces the upstream flow turbulence near the gate. This factor leads to more flow passing through the sluice gate (Figure 6). Figure 5-b shows the discharge coefficient changes in different positions relative to the vertical axis. In the upward position of the gate, the discharge coefficient is directly related to  $\theta$  and increases with increasing the  $\theta$  and vice versa. So that  $C_d$  of the gate with an angle of  $30^{\circ}$  is more than  $20^{\circ}$ ,  $10^{\circ}$  and vertical positions, respectively. On average, the sluice gate discharge coefficient in  $30^{\circ}$  is 5.88%, 12% and 16.05% higher than the  $20^{\circ}$ ,  $10^{\circ}$  and vertical positions, respectively. The flow area through the gate is constant at all angles. Also, the position of the gates leads to a change in the depth upstream of the gate, which is the most important parameter affecting the discharge coefficient. b) a)



Figure 5. Diagram a) Stage-discharge b)  $C_d$  at different angles of sluice gate

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Figure 6. Upstream flow depth and flow lines at the same discharge in different gate position

## 3.2. Downward inclined gate discharge coefficient

Figure 7-a shows the stage-discharge diagram for a sluice gate with angles of  $10^{\circ}$ ,  $20^{\circ}$  and  $30^{\circ}$ . As can be seen, increasing  $\theta$  relative to the vertical axis causes a slight increase in the depth upstream of the gate concerning the vertical position, which leads to a decrease in the discharge coefficient (Figure 7-b). On average, the gate discharge coefficient in the vertical position is 0.58%, 1.49% and 2.18% higher than the gate with angles of  $10^{\circ}$ ,  $20^{\circ}$  and  $30^{\circ}$ , respectively.



Figure 7. Diagram a) Stage-discharge b) Discharge coefficient at different angles of sluice gate

### **3.3.** Oblique gate discharge coefficient

Figure 8-a is presented for the vertical and the oblique gates relative to the transverse axis with angles of 10°, 20° and 30°. The angle of the oblique gate is inversely related to the upstream water depth. So that increasing the angle leads to reducing the water depth. According to Figure 8-a, the value of  $C_d$  increases with increasing  $y_0/G$ . In Figure 8-a, the highest  $C_d$  value



is related to the vertical gate and the lowest is related to the gate with an angle of  $30^{\circ}$ . As the angle increases, the length of the gate becomes longer than the vertical gate, which leads to an increase in the area of flow through the gate, hence the discharge coefficient reduces at greater angles. Also, this type of gate placement causes the output flow to be asymmetric under and downstream of the gate. So that, the depth and flow velocity on the sides of the gate are different from each other. Imbalance in hydraulic parameters reduces the discharge coefficient. The effect of gate length is shown in Figure 8-b. This diagram shows the effect of gate length on upstream depth and discharge coefficient. In a constant discharge and different gate lengths, the discharge coefficient of the gate with a shorter length is greater than the discharge coefficient with a longer length. b)



× Vertical Sluice Gate ▲10° oblique gate Vertical Sluice Gate 10° oblique gate 20° oblique gate • 30° oblique gate 20° oblique gate 30° oblique gate 0.63 0.63 0.61 0.61 0.59 0.59 0.57 0.57 (-) (-) (-) · PD 0.55 0.55 0.53 0.53 0.51 0.51 0.49 0.49 0.47 0.47 5 0.85 2 3 4 6 7 0.1 0.35 0.6 1.1 1.35 1.6  $y_0/G(-)$  $y_0/L(-)$ 

Figure 8. Diagram a) Stage-discharge b) Discharge coefficient at different angles of sluice gate placement

Table 5 shows the minimum, maximum and average discharge coefficient for all gate placement modes in this and previous studies. On average, the values of  $C_d$  for the upward inclined gate positions with an angle of 10°, 20° and 30° are 4.58%, 10.81% and 16.05% more than the vertical position, respectively. Also, for downward gate positions with an angle of  $10^{\circ}$  is 0.58% for gates with angles of 20° and 30°, are 1.49% and 2.18% less than the vertical position, which shows that the downward position does not have much effect on discharge coefficient. On average, for oblique gate positions with angles of 10°, 20° and 30°, 0.93%, 2.91% and 7.08% are less than the vertical position. Given that the discharge coefficient in the upward position is higher than other models, so the gate in this position can be considered the best position to increase  $C_d$ .



									Di	scharg	e Coeff	icient								
Ga	te Cases	Pr	esent stı	ıdy	Raj Sub	aratnan ramanya	n & a [2]	Raja	aratnam	[20]	Ν	lago [21	.]	H	lager [22	2]	Gate Cases	Sh Pi	ivapur akash [	* & [4]
		Max	Min	Avr	Max	Min	Avr	Max	Min	Avr	Max	Min	Avr	Max	Min	Avr	-	Max	Min	Avr
	Vertical	0.63	0.55	0.60	0.63	0.58	0.61	0.64	0.60	0.62	0.59	0.53	0.55	0.59	0.53	0.55	Vertical	0.63	0.52	0.61
Ţ,	10°	0.66	0.57	0.63	-	-	-	-	-	-	-	-	-	-	-	-	15°	0.68	0.58	0.66
line	20°	0.73	0.60	0.67	-	-	-	-	-	-	-	-	-	-	-	-	30°	0.74	0.61	0.70
Inc	30°	0.79	0.62	0.72	_	_	_	_	_	-	-	_	-	-		-	45°	0.83	0.64	0.78
	1.09	0.62	0.54	0.72														0.05	0.01	0.70
ned	10	0.05	0.54	0.60	-	-	-	-	-	-	-	-	-	-	-	-		-	-	-
ncli to I	20°	0.62	0.54	0.59	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-
∃ <sup>−</sup> 30°		0.62	0.54	0.58	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-
e	10°	0.63	0.54	0.60	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-
liqu	20°	0.62	0.53	0.58	_	-	-	-	_	-	-	_	_	-	-	-	_	-	-	-
ldO	200	0.50	0.50	0.56	_												-			
	30	0.59	0.50	0.50		-	-	-	-	-	-	-	-	-	-	-		-	-	-
							Tac	ole 6. I	lyaroo	iynan	nc ioro	e on t	ne gat	e						
											h	(kg/n	n)							
					Gate Cases															
	0										G	ale Ca	303							
N	$0  \frac{Q}{(m^{3}/s)}$	) ( <b>m</b> <sup>3</sup>	<i>q</i> <sup>3</sup> /s-m)	Vertic positic	al u on i I	10° pward nclined oosition	2 upv incl posi	0° vard ined ition	30° upwar incline positio	rd d ed on	10° lownwar inclined position	rd d	20° ownwai inclined position	rd d l	30° lownwar inclined position	d l o l p	10° blique osition	20° oblique position	30° obliq positi	ue on
N(	$O \qquad Q \\ (m^{3}/s)$	$(\mathbf{m}^3)$	<b><i>q</i></b> <b>/s-m</b> )	Vertic positio	al u on i I	10° pward nclined oosition 0.406	2 upv incl post	0° vard lined ition 295	30° upwar incline positio 0.222	rd d rd on	10° lownwar inclined position 0.995	rd d	20° ownwar inclined position 1.254	rd d I	30° lownwar inclined position 1.584	rd o l p	10° blique osition	20° oblique position 0.950	30° obliq positi 0.86	ue on j2
N(	$\begin{array}{c} 0 & Q \\ (m^3/s) \\ \hline \\ 0.0052 \\ 0.0065 \end{array}$	$(\mathbf{m}^3)$ $(\mathbf{m}^3)$	<i>q</i> b/s-m) 0264 0324	Vertic positio 0.684 1.860	al u on i I 1	10° pward nclined oosition 0.406 1.186	2 upw incl post 0.2 1.0	0° vard ined ition 295 036	30° upwar incline positio 0.222 0.722	rd d ed on 2	10° lownwar inclined position 0.995 2.557	rd d	20° ownwar inclined position 1.254 2.504	rđ d I	30° lownwar inclined position 1.584 2.746	rd l o l p <sup>r</sup> (	<b>10°</b> <b>blique</b> osition 0.975 2.417	<b>20°</b> oblique position 0.950 2.374	<b>30°</b> <b>obliq</b> <b>positi</b> 0.86 2.03	ue on 6
N(	$\begin{array}{c} Q \\ (m^{3}/s) \\ \hline \\ 0.0052 \\ 0.0065 \\ 0.0066 \\ 0.0066 \end{array}$	$(\mathbf{m}^{3})$	<i>q</i> 5/s-m) 0264 0324 0330	Vertic positio 0.684 1.860 2.238	al u on i I I J	<b>10°</b> <b>apward</b> <b>nclined</b> <b>osition</b> 0.406 1.186 1.263 0.57	2 upv incl posi 0.2 1.0 1.1	0° vard ined ition 295 036 128	<b>30°</b> upwar incline positio 0.222 0.722	rd d ed on 2 7	10° lownwar inclined position 0.995 2.557 2.757	rd d	20° ownwar inclined position 1.254 2.504 2.824	rd d l ı	<b>30°</b> lownwar inclined position 1.584 2.746 3.072	rd l p (	<b>10°</b> blique osition 0.975 2.417 2.587	20° oblique position 0.950 2.374 2.509	<b>30°</b> obliq positi 0.86 2.03 2.27	ue on 22 36 9
N(	O Q (m <sup>3</sup> /s)	$\begin{array}{c} \mathbf{m}^{3} \\ \mathbf{m}^{2} \\ \mathbf{m}^{2} \\ \mathbf{m}^{2} \\ \mathbf{m}^{2} \\ \mathbf{m}^{3} \\ \mathbf{m}$	<i>q</i> 3/s-m) 0264 0324 0330 0375	Vertic positio 0.684 1.860 2.238 4.087	al u on i I I J J	<b>10°</b> <b>apward</b> <b>nclined</b> <b>osition</b> 0.406 1.186 1.263 2.597 2.680	2 upv incl posi 0.2 1.0 1.1 2.0	0° vard ined ition 295 036 128 037	<b>30°</b> upwar incline positio 0.222 0.722 0.772 1.455	rd d rd n 2 7 2 5	10° lownwar inclined position 0.995 2.557 2.757 4.428 5.070	rd d	20° ownwar inclined position 1.254 2.504 2.824 4.984	rđ d l	<b>30°</b> lownwar inclined position 1.584 2.746 3.072 5.415 7.210	rd o l p ( 2	10° blique osition ).975 2.417 2.587 4.393	20° oblique position 0.950 2.374 2.509 4.359 5.072	<b>30°</b> obliq positi 0.86 2.03 2.27 3.99	<b>ue</b> <b>on</b> 52 66 79 73
N 1 2 3 4 5	<b>O Q</b> (m <sup>3</sup> /s)	) (m <sup>3</sup> ) 2 0.0 5 0.0 5 0.0 5 0.0	<b>q</b> 5/s-m) 0264 0324 0330 0375 0404	Vertic positio 0.684 1.860 2.238 4.082 5.556	<b>al u</b> <b>jon i</b> <b>k</b> 4 ) 3 7 5 5	<b>10°</b> <b>pward</b> <b>nclined</b> <b>osition</b> 0.406 1.186 1.263 2.597 3.689 7.604	2 upw incl post 0.2 1.0 1.1 2.0 2.8	0° vard ined ition 295 036 128 037 815 412	<b>30°</b> <b>upwar</b> <b>incline</b> <b>positio</b> 0.222 0.722 0.772 1.455 1.990	rd d rd 9 7 2 5 1	10° lownwar inclined position 0.995 2.557 2.757 4.428 5.970	rd d	20° ownwar inclined positior 1.254 2.504 2.824 4.984 6.762	rd d I 1	<b>30°</b> lownwar inclined position 1.584 2.746 3.072 5.415 7.319	rd 0   0   p   (   	10° blique osition 0.975 2.417 2.587 4.393 6.028 2.082	20° oblique position 0.950 2.374 2.509 4.359 5.978	<b>30°</b> <b>obliq</b> <b>positi</b> 0.86 2.03 2.27 3.99 5.52	ue on 22 66 99 33 .11
N 1 2 3 4 5 6	<b>O Q</b> (m <sup>3</sup> /s)	2 0.0 5 0.0 5 0.0 5 0.0 5 0.0 0 0.0 6 0.0	<i>q</i> 5/s-m) 0264 0324 0330 0375 0404 0481	Vertic positio 0.684 1.860 2.238 4.08 5.550 11.21	al u on i I 4 ) 3 7 5 5	<b>10°</b> <b>pward</b> <b>nclined</b> <b>osition</b> 0.406 1.186 1.263 2.597 3.689 7.604 0.150	2 upw incl post 0.2 1.0 1.1 2.0 2.8 6.2	0° vard iined ition 295 036 128 037 815 412	<b>30°</b> <b>upwar</b> <b>incline</b> <b>positio</b> 0.222 0.722 1.455 1.990 4.746	d d d 2 7 2 5 )	10° lownwar inclined position 0.995 2.557 2.757 4.428 5.970 12.402	rd d	20° ownwar inclined positior 1.254 2.504 2.824 4.984 6.762 14.348	rd d l	<b>30°</b> lownwar inclined position 1.584 2.746 3.072 5.415 7.319 18.705	rd 0 1 P ( 2 2 2 4 ( 1	10° blique osition 0.975 2.417 2.587 4.393 6.028 2.083 4.115	20° oblique position 0.950 2.374 2.509 4.359 5.978 11.207 12.671	<b>30°</b> obliq positi 0.86 2.03 2.27 3.99 5.52 10.53	ue on 22 66 99 33 11 855
N 1 2 3 4 5 6 7	Q (m³/s)           0.0052           0.0065           0.0066           0.0066           0.0075           0.0086           0.0096           0.0096           0.0097           0.0096	$\begin{array}{c} \mathbf{m}^{2} \\ \hline \mathbf{m}^{2} \\ \mathbf{m}^{2} \\ \hline \mathbf{m}^{2} \\ \hline \mathbf{m}^{2} \\ \hline \mathbf{m}^{2} \\ \mathbf{m}^{2} \\ \hline \mathbf{m}^{2} \\ \mathbf{m}^{2} \\ \hline \mathbf{m}^{2} \\ \hline \mathbf{m}^{2} \\ \hline \mathbf{m}^{2} \\ \hline \mathbf{m}$	<i>q</i> b/s-m) 0264 0324 0330 0375 0404 0481 0499 0530	Vertic positic 0.684 1.860 2.238 4.08 5.556 11.21 13.08	al u on i 4 ) 3 7 5 5 4 3	10° pward nclined osition 0.406 1.186 1.263 2.597 3.689 7.604 9.159	2 upw incl posi 0.2 1.0 1.1 2.0 2.8 6.4 7.2 7.2	0° vard ined ition 295 036 128 037 815 412 219 340	<b>30°</b> <b>upwar</b> <b>incline</b> <b>positio</b> 0.222 0.772 1.455 1.990 4.746 4.808	rd d ed n 2 7 2 5 5 3 3 3 2	10° lownwar inclined position 0.995 2.557 2.757 4.428 5.970 12.402 14.257 18.714	rd d	20° ownwal inclined position 1.254 2.504 2.824 4.984 6.762 14.348 16.348 21.125	rd d l	<b>30°</b> lownwar inclined position 1.584 2.746 3.072 5.415 7.319 18.705 19.322 23.50°	rd 0 1 P 1 ( 2 2 2 2 1 1	10° blique osition 0.975 2.417 2.587 4.393 5.028 2.083 4.115 7 898	20° oblique position 0.950 2.374 2.509 4.359 5.978 11.207 12.671 12.668	<b>30°</b> obliq positi 0.86 2.03 2.27 3.99 5.52 10.55 12.20	ue on 22 66 99 13 11 85 668 23
N( 1 2 3 4 5 6 6 7 8	Q (m³/s)           0.0052           0.0065           0.0066           0.0066           0.0075           0.0086           0.0096           0.0096           0.0110	(m <sup>3</sup> )       2     0.0       5     0.0       5     0.0       5     0.0       5     0.0       5     0.0       5     0.0       6     0.0	<b><i>q</i></b> (ys-m) (0264 (0324 (0330) (0375) (0404 (0481) (0499) (0530) (0559)	Vertic positic 0.684 1.860 2.233 4.08 5.556 11.21 13.08 17.599 21.44	<b>al u</b> <b>m i</b> 4 ) 3 7 5 5 4 3 4	10° mpward nclined osition 0.406 1.186 1.263 2.597 3.689 7.604 9.159 11.810 1.6 886	2 upw incl posi 0.2 1.0 1.1 2.0 2.8 6.4 7.2 9.3	0° vard ined ition 295 036 128 037 815 412 219 349 349	<b>30°</b> <b>upwar</b> <b>incline</b> <b>positio</b> 0.222 0.727 0.772 1.455 1.990 4.746 4.808 6.433 7.818	rd d rd 2 7 2 5 5 3 3 3 2	10° lownwar inclined position 0.995 2.557 2.757 4.428 5.970 12.402 14.257 18.714 23.741	rd d	20° ownwar inclined position 1.254 2.504 2.824 4.984 6.762 14.348 16.348 21.135 26.611	rd d l	<b>30°</b> lownwar inclined position 1.584 2.746 3.072 5.415 7.319 18.705 19.322 23.598 23.598	rd o p ( ( ( ( 1 1 1 1	10° blique osition 0.975 2.417 2.587 4.393 5.028 2.083 4.115 7.898 1.927	20° oblique position 0.950 2.374 2.509 4.359 5.978 11.207 12.671 15.968 19.859	<b>30°</b> obliq positi 0.86 2.03 2.27 3.99 5.52 10.55 12.20 15.42	<b>ue</b> on 22 66 99 33 11 855 68 23 34
N( 1 2 3 4 5 6 7 7 8 9	Q         (m³/s)           0         0.0052           2         0.0062           3         0.0066           4         0.0075           5         0.0086           6         0.0096           7         0.0096           6         0.0166           9         0.0116           0         0.0116	$\begin{array}{c} \mathbf{m}^{3} \\ \mathbf{m}^{2} \\ \mathbf{m}$	<b>q</b> //s-m) 0264 0324 0330 0375 0404 0481 0499 0530 0559 0559	Vertic positic 0.684 1.860 2.233 4.08 5.550 11.21 13.08 17.59 21.44 25.96	<b>al u</b> <b>F</b> <b>1</b> <b>1</b> <b>1</b> <b>1</b> <b>1</b> <b>1</b> <b>1</b> <b>1</b> <b>1</b> <b>1</b>	10° mpward nclined osition 0.406 1.186 1.263 2.597 3.689 7.604 9.159 11.810 16.886 18,707	2 upw incl post 0.2 1.0 2.8 6.4 7.2 9.3 11.	0° vard ined ition 295 036 128 037 815 412 219 349 395 524	<b>30°</b> <b>upwar</b> <b>incline</b> <b>positio</b> 0.222 0.727 1.455 1.990 4.746 4.808 6.433 7.818 8.290	rd d vd 2 7 2 5 ) 5 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3	10° lownwar inclined position 0.995 2.557 2.757 4.428 5.970 12.402 14.257 18.714 23.741 23.741	rd d	20° ownwar inclined position 1.254 2.504 2.824 4.984 6.762 14.348 16.348 21.135 26.611 33.501	rd d I	<b>30°</b> lownwar inclined position 1.584 2.746 3.072 5.415 7.319 18.705 19.322 23.598 29.168 34.823	rd o p ( ( 1 1 1 2 2 2	10° blique osition 0.975 2.417 2.587 4.393 5.028 2.083 4.115 7.898 1.927 6.310	20° oblique position 0.950 2.374 2.509 4.359 5.978 11.207 12.671 15.968 19.859 23.019	<b>30°</b> obliq positi 0.86 2.03 2.27 3.99 5.52 10.53 12.20 15.44 18.92	ue on 22 66 99 33 11 85 668 223 34 57

Table 5. Comparison of discharge coefficient of the present study with previous studies

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Table 6 shows the hydrodynamic force applied to the sluice gate in all different models and discharges. Examination of the results indicated that increasing the discharge rate increases the hydrodynamic force on the gate, which is also due to the increase in the upstream depth of the gate. This increase in depth increases the pressure and force on the gate. Comparison of the results showed that the hydrodynamic force on the gate has the lowest value in the upward gate position and the highest value related to the downward position. So that by increasing the angle with respect to the vertical axis upstream of the channel, the hydrodynamic force decreases. In the case of oblique gates, the upstream depth decreases with increasing angle and therefore the hydrodynamic force decreases.

#### 4. Conclusion

In the present study, the hydraulic parameters of the sluice gate, including discharge coefficient  $(C_d)$  and hydrodynamic force on the gate in different positions, including upward and downward deviation and oblique position were investigated using FLOW-3D software. The simulations were performed in the discharge range of 0.0053 to 0.012 m<sup>3</sup>/s. The RNG turbulence model showed acceptable results in terms of accuracy in model simulation and the results obtained between the numerical solution and experimental in comparison with other turbulence models such as k- $\varepsilon$ , k- $\omega$  and LES. To validate the model and achieve the desired mesh, several simulations with different mesh dimensions were performed. By examining the results of statistical indicators with different mesh dimensions, mesh blocks with nested mesh dimensions of 0.8 and 0.4 cm were selected as the optimal mesh. The results showed that the upward inclined gate has a higher discharge coefficient compared to other gate models. The maximum  $C_d$  is for an upward inclined gate with an angle ( $\theta$ ) of 30° with a quantity of 0.79. On average, the gate discharge coefficient in the  $30^{\circ}$  upward position is 5.88%, 12% and 16.05% higher than the  $20^{\circ}$  and  $10^{\circ}$  upward and vertical positions, respectively. The results showed that the hydrodynamic force on the gate decreases in the upward inclined position with increasing  $\theta$ . This value is inverted for the downward inclined gate position and increases with increasing  $\theta$ . So that, the hydrodynamic force on the gate in the vertical position is less than the gate with an angle of 30° to the downstream of the channel. The discharge coefficient for the downward inclined gate does not change significantly with increasing  $\theta$ . In the case of oblique gate, increasing  $\theta$  leads to an increase in the area of flow through the gate and also decreases the upstream fluid depth, so the discharge coefficient was lower than in the vertical position.  $30^{\circ}$ upwards inclined gate showed 16.67% and 22.22% higher discharge coefficient than the vertical and 30° downward gate positions, respectively.

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